

rk: HW 1.3

1 2 3 4 5 6 7 8 9 10

Score: 0 of 1 pt

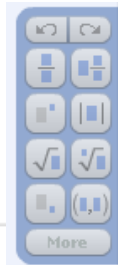
HW Score: 0% (0 of 10 pts)

0 of 10

(a) Find a simplified form of the difference quotient and (b) complete the following table.

$$f(x) = 2x^2$$

$$f'(x) = 4x$$



x	h	$\frac{f(x+h) - f(x)}{h}$
5	2	$20 + 2h = 24$
5	1	$20 + 2h = 22$
5	0.1	$20 + 2h = 20.2$
5	0.01	$20 + 2h = 20.02$

a) $\frac{f(x+h) - f(x)}{h} = \square$

D.Q.

$$f(x+h) = 2(x+h)^2$$

$$= 2(x^2 + 2xh + h^2) = 2x^2 + 4xh + 2h^2$$

$$a) \frac{f(x+h) - f(x)}{h} = \frac{2x^2 + 4xh + 2h^2 - 2x^2}{h}$$

$$= \frac{h(4x + 2h)}{h} = 4x + 2h$$

$$(a+b)^2 = a^2 + 2ab + b^2$$

Compute the difference quotient $\frac{f(x+h) - f(x)}{h}$ for the function $f(x) = \frac{8}{x+10} = 8(x+10)^{-1}$

$\frac{f(x+h) - f(x)}{h} = \square$

$f'(x) = -8(x+10)^{-2} = \frac{-8}{(x+10)^2}$

$f(x+h) = \frac{8}{(x+h)+10}$

$$\begin{aligned} \frac{f(x+h) - f(x)}{h} &= \left(\frac{8}{x+h+10} - \frac{8}{x+10} \right) \cdot \frac{1}{h} \\ &= \frac{8(x+10) - 8(x+h+10)}{(x+h+10)(x+10)} \cdot \frac{1}{h} \\ &= \frac{8x + 80 - 8x - 8h - 80}{(x+h+10)(x+10)} \cdot \frac{1}{h} \\ &= \frac{-8h}{(x+h+10)(x+10)} \cdot \frac{1}{h} \\ &= \frac{-8}{(x+h+10)(x+10)} \end{aligned}$$

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Ex. Score: 0 of 1 pt

HW Score: 0% (0 of 10 pts)

Compute the difference quotient $\frac{f(x+h) - f(x)}{h}$ for the function $f(x) = -4x^2 - 3x - 4$

$$f'(x) = -8x - 3$$

$$\frac{f(x+h) - f(x)}{h} = \square$$

$$\begin{aligned} f(x+h) &= -4(x+h)^2 - 3(x+h) - 4 \\ &= -4(x^2 + 2xh + h^2) - 3x - 3h - 4 \\ &= -4x^2 - 8xh - 4h^2 - 3x - 3h - 4 \end{aligned}$$

$$\begin{aligned} \frac{f(x+h) - f(x)}{h} &= \frac{-4x^2 - 8xh - 4h^2 - 3x - 3h - 4 - (-4x^2 - 3x - 4)}{h} \\ &= \frac{-4x^2 - 8xh - 4h^2 - 3x - 3h - 4 + 4x^2 + 3x + 4}{h} \\ &= \frac{-8xh - 4h^2 - 3h}{h} \\ &= \frac{h(-8x - 4h - 3)}{h} = -8x - 4h - 3 \end{aligned}$$

An object dropped from rest from the top of a tall building on Planet X falls a distance $d(t) = 20t^2$ feet in the first t seconds. Find the average rate of change of distance with respect to time as t changes from $t_1 = 4$ to $t_2 = 7$. This rate is known as the average velocity, or speed.

The average velocity as t changes from 4 to 7 seconds is $\frac{\text{feet}}{\text{sec}}$.

$$\begin{matrix} x_1 & \text{to} & x_2 \\ \frac{f(x_2) - f(x_1)}{x_2 - x_1} \end{matrix}$$

$$\text{avg vel.} = \frac{\Delta \text{ distance}}{\Delta \text{ time}}$$

$$= \frac{d(t_2) - d(t_1)}{t_2 - t_1}$$

$$= \frac{d(7) - d(4)}{7 - 4}$$

$$= \frac{980 - 320}{3} = \frac{660}{3} = 220 \frac{\text{ft}}{\text{sec}}$$